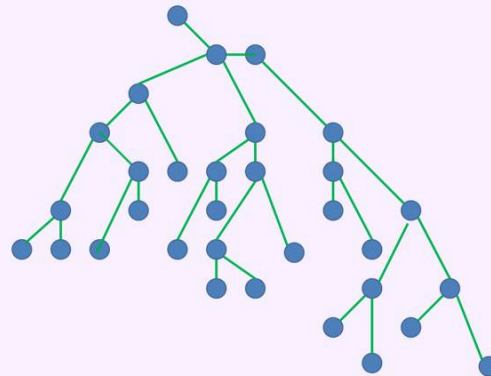
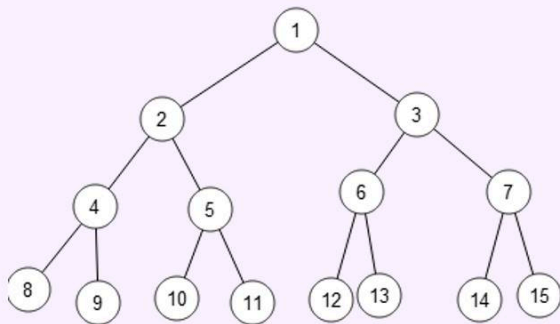


Announcements

MP4 available, due 3/10/17, 11:59p. EC due 3/3/17, 11:59p.

SINCE WHEN

Is this more attractive **than this?**



End the impossible standards set by society. All Trees Are *Perfect*.

Complete Binary tree: for any level k in $[0, h-1]$, level k has 2^k nodes, and on level h , all nodes are "pushed to the left."

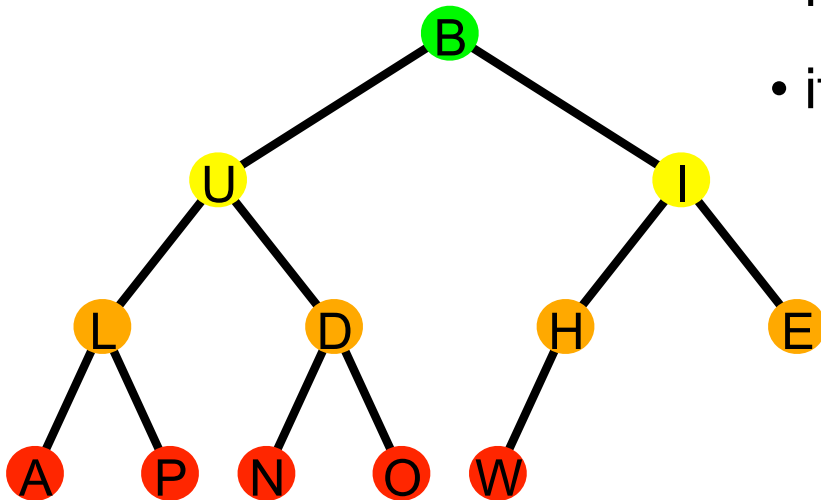
Complete tree of height h , C_h :

- if $h = -1$, then C_h is $\{\}$
- if $h > -1$, then C_h is $\{r, T_L, T_R\}$, and either:

T_L is _____ and T_R is _____

OR

T_L is _____ and T_R is _____



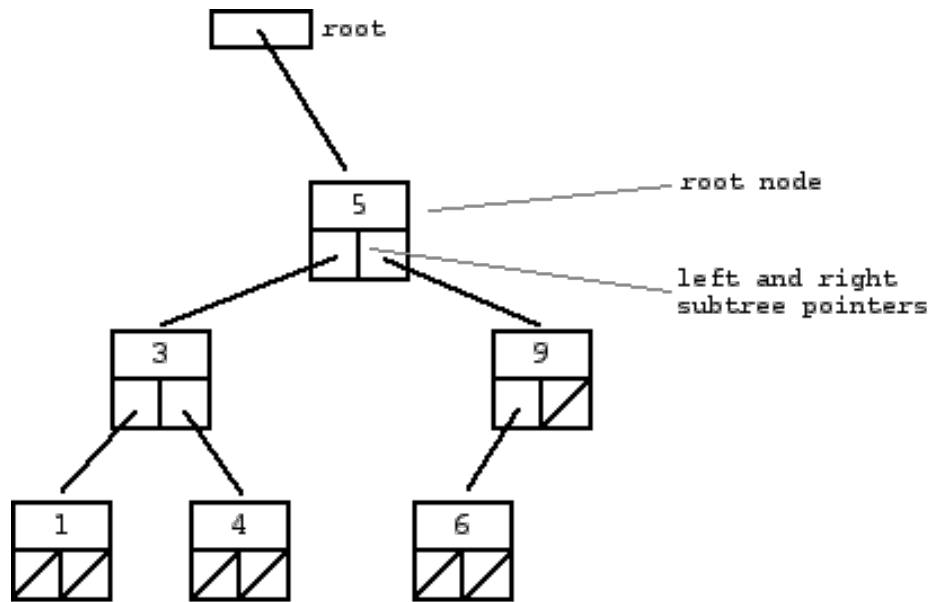
<http://xlinux.nist.gov/dads//HTML/completeBinaryTree.html>

Check for understanding:

Is every full tree complete?

Is every complete tree full?

Rooted, directed, ordered, binary trees



Tree ADT:

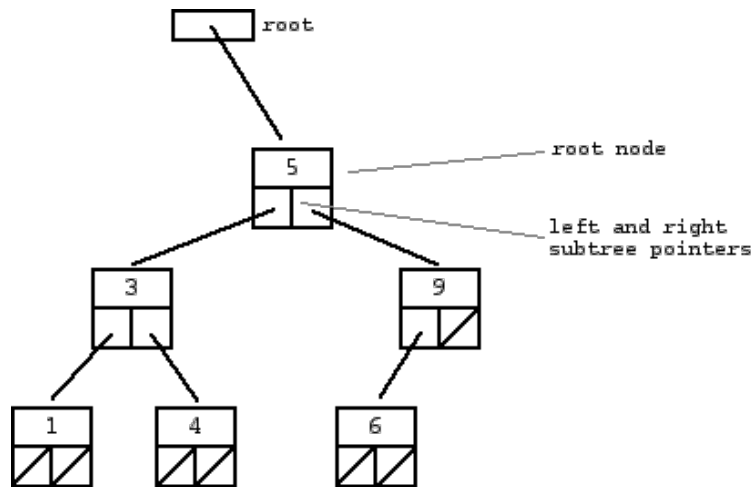
insert

remove

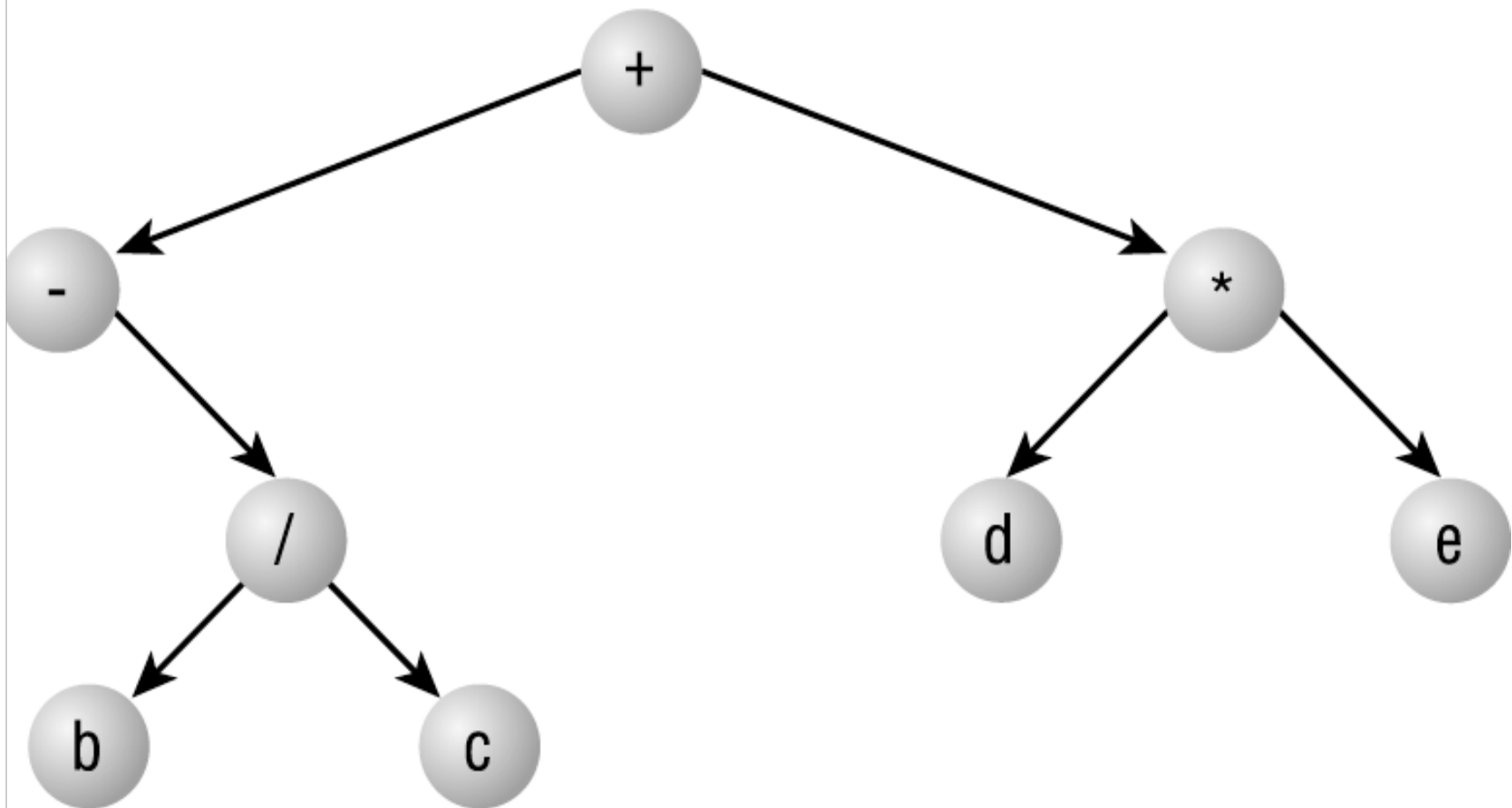
traverse

```
template <class T>
class tree{
public:
...
private:
    struct treeNode{
        T data;
        treeNode * left;
        treeNode * right;
    };
    treeNode * root
...
};
```

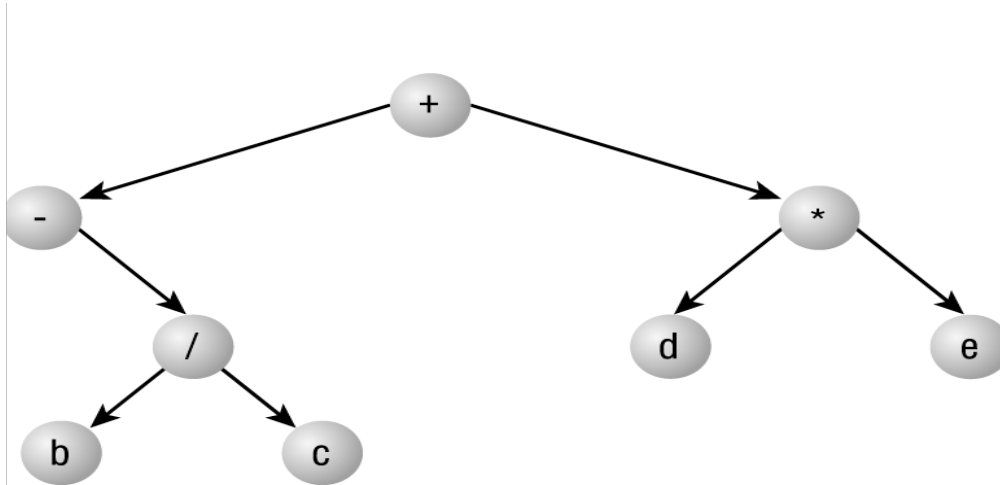
Theorem: if there are n data items in a binary tree, then there are _____ null pointers.



Traversals



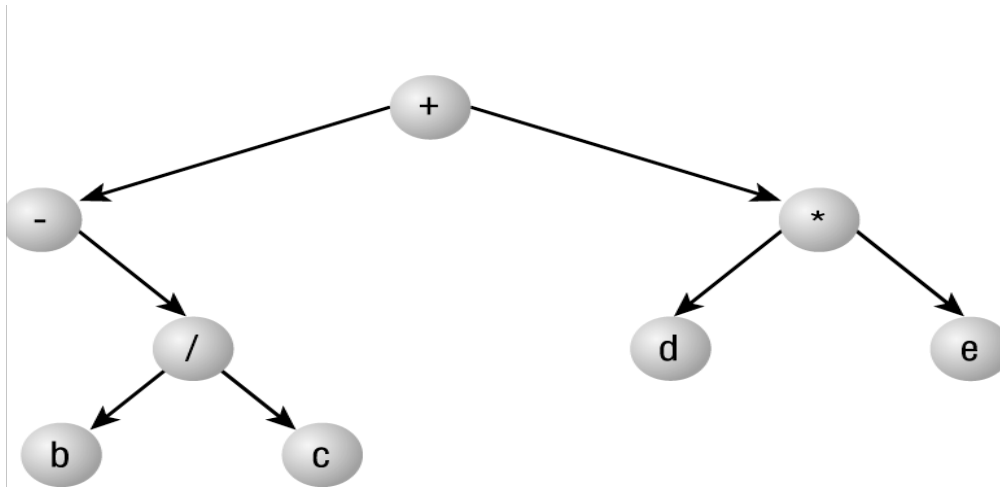
Traversals: A few discussion points...



```
template<class T>
void binaryTree<T>::__Order(treeNode * croot){
    if (croot != null){
        _____
        _____Order(croot->left);
        _____
        _____Order(croot->right);
        _____
    }
}
```

1. Where is the base case?

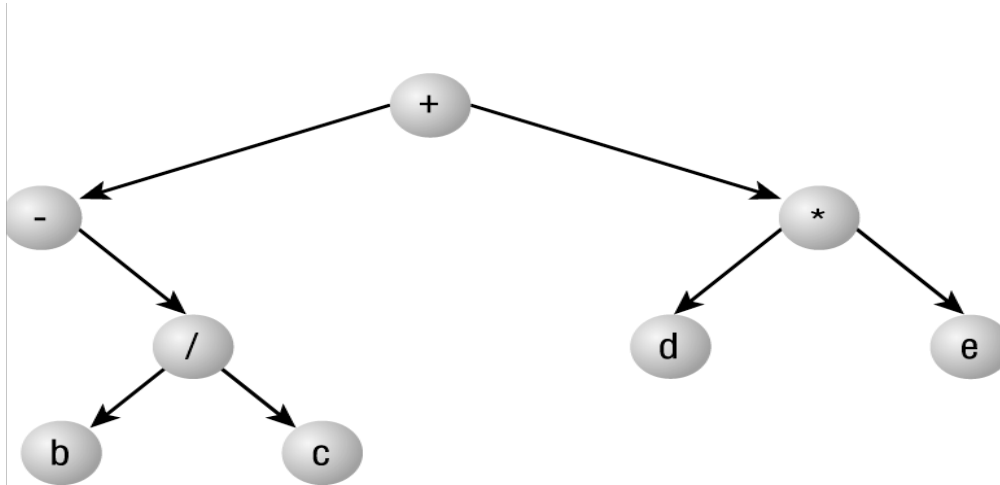
Traversals: A few discussion points...



```
template<class T>
void binaryTree<T>::__Order(treeNode * croot){
    if (croot != null){
        _____
        _____Order(croot->left);
        _____
        _____Order(croot->right);
        _____
    }
}
```

2. Running time?

Traversals: A few discussion points...



```
template<class T>
void binaryTree<T>::__Order(treeNode * croot){
    if (croot != null){
        _____
        _____Order(croot->left);
        _____
        _____Order(croot->right);
        _____
    }
}
```

3. Is this function public or private?